MÖSSBAUER STUDIES OF IRON-BASED SUPERCONDUCTORS

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ABSTRACT
This contribution attempts to be a review concerned with the microscopic characterization of complex materials by using transmission Mössbauer spectroscopy – mainly 14.4-keV resonant transition in \(^{57}\)Fe. An attention is focused on the novel superconductors, i.e. iron-based superconductors, the latter being extensively investigated in our Mössbauer laboratory primarily versus sample temperature. Iron-based superconductors make four major families based on the corrugated nearly two-dimensional sheets of either strongly bound iron-pnictogen or iron-chalcogen atoms. Usually, superconductivity is induced by doping or applying pressure to the parent compound except the simplest compounds of the ‘11’ family. One can dope any kind of atom within the compound in isovalent, hole-doping or electron-doping fashion. Parent compounds exhibit itinerant magnetic order of the 3d (iron) character. It appears as spin density wave (SDW) of the antiferromagnetic type incommensurate with the respective lattice period and of the complex shape. For majority of cases it is longitudinal SDW propagating along the a-axis of the orthorhombic unit cell being created at the magnetic order from the tetragonal cell – due to the magneto-elastic forces. On the other hand, the 3d magnetism and orthorhombic distortion are gone for superconductors as shown by Mössbauer spectra obtained versus temperature, and by spectra obtained in the strong external magnetic field at low temperatures – stronger than the first critical field for these second kind superconductors. However, superconductivity is intimately related to these layered structures with the electronic charge modulation leading to the charge density wave (CDW) on iron nuclei – observed as variation of the isomer shift. What is more, one observes closely related modulation of the electric field gradient on iron nuclei called electric field gradient wave (EFGW). The shape of these modulations changes rapidly at the superconducting gap opening and relaxes back once the bosonic system of Cooper pairs is fairly well separated from the rest of the electronic system. It was found that localized 4f magnetic moments order within superconducting phase in a similar fashion as in the normal phase. Keywords: iron-based superconductors, Mössbauer spectroscopy, charge density wave, electric field gradient wave

1 INTRODUCTION
Usually 3d magnetic order and superconductivity are mutually exclusive within the same electronic system – particularly ferromagnetic type of order and s-type superconductivity. However, diamagnetic forms of iron exist and are able to form stable compounds. The majority of these compounds have large energy gap and respective compounds are insulators or semi-conductors at best [1]. Hence, they cannot exhibit superconductivity. A small group of iron compounds is simultaneously metallic and diamagnetic as far as 3d magnetism is considered. Hence, they might become superconductors at low temperatures. Even pure iron in the hexagonal ε-form exhibits superconducting island, albeit upon having applied hydrostatic pressure [2]. On the other hand, it is easily magnetically polarized in the strong external magnetic field. A discovery of layered iron-based unconventional superconductors in 2008 by the Hosono team was a real breakthrough [3]. They have many similarities to cuprates [4], albeit exhibit many differences, as the parent compounds are metallic and exhibit
itinerant 3d antiferromagnetism. The common feature for all iron-based superconductor families is presence of strongly coupled iron-pnictogen or iron-chalcogen layers with tetrahedral iron coordination within the layer. Hence, the iron occurs nominally in the divalent state [5]–[7]. There are four major families of these compounds excluding some more complex derivatives. All of them crystallize in the tetragonal symmetry, and parent compounds undergo orthorhombic distortion closely related to the 3d magnetic order. The simplest is ‘11’ family being just a stack of FeSe layers. This compound has no parent and exhibits superconductivity below about 8 K under normal pressure, albeit orthorhombic distortion occurs at much higher temperature [8]. The ‘111’ family differs by intercalation of iron-chalcogen layers by some diamagnetic ions like lithium [9]. Much higher superconducting transition temperatures could be obtained for ‘11’ and ‘1111’ families. The parent compound of the ‘111’ family has composition AFe$_2$As$_2$ with A being some metal including magnetic 4f elements with either almost pure spin magnetic moment like Eu$^{2+}$ or Gd$^{3+}$ ions or ions having significant orbital contribution to the magnetic moment. 4f magnetic moments remain highly localized, if present. Large, almost perfect single crystals of the ‘111’ family compounds could be grown. It is interesting to note, that two adjacent FeAs layers within ‘111’ compounds are mutually inverted, while for remaining families simple stacking occurs. The ‘1111’ family has larger separation between FeAs layers as the separator is made of cation and anion like for example in PrFeAsO. The parent compound could be converted into superconductor by replacement of any element, i.e., by hole, electronic or isovalent doping. One can apply hydrostatic pressure as well [10]. Upon doping 3d magnetism diminishes, transition to the orthorhombic phase disappears, and superconductivity occurs. For the majority of cases there is some optimal doping. For overdoped material a transition temperature to the superconducting state lowers and eventually disappear leading to the metallic and 3d diamagnetic state [11]–[12]. Larger separation between iron bearing layers leads to higher superconducting transition temperatures due to reduced dimensionality [13]. Macroscopic measurements show some coexistence of the 3d magnetic order and superconductivity for underdoped samples.

Resonant transition of 14.4-keV between ground and first excited state of $^{57}$Fe is the best Mössbauer transition from the experimental point of view. Natural iron contains about 2.14 at. % of $^{57}$Fe and it is a major constituent of the compounds described above. Hence, it seems natural to use transmission Mössbauer spectroscopy to look upon local properties of iron-based superconductors. One can look upon hyperfine interactions of the iron nucleus and get some information about dynamics from the recoilless fraction and second order Doppler shift (SOD). Resonant transition of 21.6-keV connecting ground and first excited state of $^{151}$Eu could be used as well for compounds bearing europium as natural europium contains about 47.8 at. % of $^{151}$Eu.

2 BASIC FEATURES OF MÖSSBAUER SPECTROSCOPY

For time independent Mössbauer spectra one can get information on the dynamics of the resonant atom via measured recoilless fraction and SOD. On the other hand, much more information yields hyperfine interactions including isomer shift, electric quadrupole interaction and eventually magnetic dipole interaction. Resolution of the 14.4-keV transition in $^{57}$Fe is good enough to derive information on the hyperfine magnetic field modulation, and to some limited extent on the electronic charge distribution on the resonant sites.
2.1 Hyperfine interactions

Basically one observes the following hyperfine interactions: 1) the isomer shift due to the finite electron density within resonant nucleus, 2) electric quadrupole interaction, and 3) magnetic dipole interaction. The isomer shift is expressed as \( \delta = \alpha (\rho_1 - \rho_2) \) with the parameter \( \alpha \) being calibration constant for a given resonant transition, \( \rho_1 \) denoting electron density on the resonant nucleus, and \( \rho_2 \) standing for corresponding density in the adopted standard. For 14.4-keV transition in \(^{57}\text{Fe}\) on \( \text{e} \) has \( \rho_1 = 3.29(2) \text{ el. a.u.} \) and adopted standard is natural metallic \( \alpha\text{-Fe} \) at room temperature with about \( 3.2 \text{ el./a.u.} \) neglecting thermal expansion [14].

The electric quadrupole interaction is caused by the interaction between nuclear spectroscopic electric quadrupole moment and the electric field gradient on the nucleus. The electric field gradient (EFG) tensor field could be expressed in terms of the stationary electric charge distribution in the following way [15]:

\[
V(r) = \frac{3}{4 \pi \varepsilon_0} \int_0^{2\pi} d\phi \int_0^\pi d\theta \sin \theta \left( \begin{array}{ccc}
\sin^2 \theta \cos^2 \phi - \frac{1}{3} & \sin^2 \theta \sin \phi \cos \phi & \sin \theta \cos \theta \cos \phi \\
\sin^2 \theta \sin \phi \cos \phi & \sin^2 \theta \sin^2 \phi - \frac{1}{3} & \sin \theta \cos \theta \sin \phi \\
\sin \theta \cos \theta \cos \phi & \sin \theta \cos \theta \sin \phi & \cos^2 \theta - \frac{1}{3}
\end{array} \right) \int_{R_0}^{\infty} \frac{dR}{R^3} \rho(r + R)
\]

with \( R = R \left( \begin{array}{c}
\sin \theta \cos \phi \\
\sin \theta \sin \phi \\
\cos \theta
\end{array} \right) \).

(1)

Here the symbol \( \varepsilon_0 \) denotes electric permeability of vacuum. Eventual charge of the probing nucleus is excluded from calculations, while the exclusion zone (eventually containing probing nucleus) described by the radius \( R_0 \) contains remaining charge having nearly spherical symmetry (except eventual linear terms do not contributing to the EFG tensor), and hence do not contributing to the EFG, as one needs symmetry lower than cubic (around given point) to have non-zero EFG. The integral is convergent for large distances as the matter is neutral on sufficiently large scales. The symbol \( \rho(r + R) \) denotes total density of the electric charge. One can see that the EFG tensor is symmetric and traceless. Hence, it can be always diagonalized locally and it is invariant upon axes inversion. It has axial symmetry provided a three fold or four fold axis is present at the point considered \( r \). For a local diagonal representation one can write the following expression:
The so-called asymmetry parameter \( \eta = (V_{11} - V_{22})/V_{33} \) satisfies the following condition \( 0 \leq \eta \leq 1 \) provided one has \( |V_{11}| \leq |V_{22}| \leq |V_{33}| \) and \( V_{33} \neq 0 \). For axially symmetric EFG one has \( \eta = 0 \). The electric quadrupole part of the hyperfine Hamiltonian takes on the following form in above principal coordinates:

\[
H_Q = A_Q \left[ 3I_z^2 - I^2 + \eta (I_z^2 - I_1^2) \right]
\]

with \( A_Q = \left( \frac{eQV_{33}}{4I(2I-1)} \right)(c/E_0) \) or

\[
H_Q = \left( \frac{eQ}{2I(2I-1)} \right)(c/E_0)(I \cdot V \cdot I) , I = \begin{pmatrix} I_1 \\ I_2 \\ I_3 \end{pmatrix}.
\]

Here the symbol \( e \) denotes positive elementary charge, the symbol \( Q \) stands for spectroscopic nuclear quadrupole moment in a given nuclear state, the symbol \( I \) denotes spin of this nuclear state, \( c \) stands for speed of light in vacuum, and \( E_0 \) denotes resonant transition energy. The symbols \( I_1, I_2, I_3 \) denote nuclear spin projection operators on respective Cartesian axes. The symbol \( I^2 \) stands for \( I_1^2 + I_2^2 + I_3^2 \). One can note that splitting could be observed provided \( I > \frac{1}{2} \). Hence, no quadrupole interaction is seen in the ground state of \( ^{57}\text{Fe} \) with \( I_z = \frac{1}{2} \), and a doublet is created in the first excited state with \( I_z = \frac{3}{2} \). The spectroscopic moment for this state amounts to \( Q_z = +0.17(1) \text{ b} \). The splitting of this state amounts to \( \Delta = 2 |e| \) with \( e = \frac{1}{4}Q_V V_{33} (c/E_0) \sqrt{1 + \eta^2}/3 \).

Magnetic dipole interaction could be described in the point-like approximation for 14.4-keV transition in \( ^{57}\text{Fe} \). It occurs provided some magnetic order exists unless some external field is applied. The ground state splits into two levels, while the excited into four levels. Usually one sees six lines unless excited state Hamiltonian is highly non-diagonal due to the large and misaligned EFG as the transition is almost pure M1 transition. The occupation of the ground state sub-levels could be assumed as being equal each other unless extremely low temperatures occur. Magnetic part of the hyperfine Hamiltonian could be written in the following form in coordinates defined in previous paragraph:

\[
H_M = - \mu_N gB \left( \frac{c}{E_0} \right) \left[ I_z \cos \beta + \sin \beta (I_1 \cos \gamma + I_2 \sin \gamma) \right] \text{or} \quad H_M = - \mu_N g \left( \frac{c}{E_0} \right)(B \cdot I).
\]

The symbol \( \mu_N \) denotes nuclear magneton. The symbol \( g \) stands for the gromagnetic factor of the given nuclear state, while the symbol \( B \) denotes value of the
total magnetic field acting on the nucleus. Angles $\beta$ and $\gamma$ stand for the polar and azimuthal angles, respectively, of the hyperfine field axial vector $B$ in the coordinates used. One has magnetic Hamiltonian solely for the ground state, while for the excited state one obtains $H = H_0 + H_M + S I$ with $S$ being a total shift due to the isomer shift and SOD. For small EFG one can write eigenvalues of the excited state in the following approximate form provided the magnetic interaction dominates:

$$
\langle m_s | H | m_s' \rangle =
\delta_{m_s m_s'}
- \mu_N g_J B \left( \frac{e Q V_3}{24 E_\gamma} \right) m_s + \left( \frac{e Q V_3}{24 E_\gamma} \right) [3 \cos^2 \beta - 1 + \eta \sin^2 \beta \cos(2\gamma)] (3m_s^2 - \frac{1}{3}) + S.
$$

(5)

Here the symbols $m_s$ and $m_s'$ denote nuclear magnetic quantum numbers. The electric quadrupole interaction apparently vanishes for the so-called magic angle $\beta = 54.74^\circ$ within this approximation provided $\eta = 0$. The sign of the quadrupole coupling constant could be determined in the presence of the magnetic splitting (here practically in the case of axially symmetric EFG). Expression (5) allows to find extremely small electric quadrupole interaction – particularly for $\beta = 0$ [16].

### 2.2 Modulated structures

The simplest modulated structure is a 3d itinerant magnetism with the magnetic moment (hyperfine field) varying along some crystal direction. Such modulation is called spin density wave (SDW) and it could be longitudinal (moments aligned with the modulation direction), perpendicular or mixed. For the perpendicular case one can expect various forms of fans or spirals. The SDW is quite often incommensurate with the respective lattice period. Hence, various resonant nuclei experience various hyperfine fields. Usually the modulation is some form of interlaced antiferromagnetic structures. Such structures become commensurate provided the number of the space dimensions is suitably increased.

Another form could be atomic positions in quasi-crystals or charge modulation (charge density wave – CDW) leading eventually to the respective modulation of the EFG (electric field gradient wave – EFGW). In general, modulated field $A(r)$ versus position $r$ could be expanded in the plane waves of the form [15], [17]:

$$
A(r) = \sum_{k} \sum_{n=1}^{N(K)} \left\{ a_{kn}(r) \cos (n \cdot q_k \cdot r) + b_{kn}(r) \sin (n \cdot q_k \cdot r) \right\} ; \quad K \geq 1 \ , \quad N(K) \geq 1.
$$

(6)

The index $k$ enumerates various field components, while the index $n$ respective harmonics of these components with the even amplitudes $a_{kn}(r)$ and eventual corresponding odd components $b_{kn}(r)$. For the majority of cases one can assume that above amplitudes do not depend on current position $r$. Each sub-field might have characteristic wave vector. Resonant transition of 14.4-keV in $^{57}$Fe is very sensitive to the shape of the SDW. Sinusoidal SDW with small admixture of higher harmonics is
observed in chromium, while the original idea of this type of order is due to Overhauser.

In the case of CDW and/or EFGW some approximations are usually needed due to the limited resolution of the method. The EFGW is usually approximated as distribution of the parameter \(\varepsilon = \frac{Q}{V} \sqrt{\frac{\varepsilon}{E_0}} \sqrt{1 + \eta^2 / 3}\) in the following form

\[
\varepsilon(q \cdot r) = \varepsilon_0 + AF_{\text{max}}^{-1} F(q \cdot r).
\]

The parameter \(\varepsilon_0\) describes eventual constant component. The parameter \(A\) denotes amplitude of the modulation, while the parameter \(F_{\text{max}}\) is the maximum of the function \(F(q \cdot r)\). The latter function takes on the following form [18]:

\[
F(q \cdot r) = \sin(q \cdot r) \left\{ \exp \left[ -\beta^2 \frac{(q \cdot r - \frac{1}{4})^2}{\rho} \right] + \exp \left[ -\beta^2 \frac{(q \cdot r - \frac{3}{4})^2}{\rho} \right] \right\}.
\]

The phase angle covers the range \(0 \leq q \cdot r < 2\pi\) (quite often range \(0 \leq q \cdot r \leq \pi\) suffices), while the parameter \(\beta\) is responsible for the shape. In the case of CDW one can usually estimate dispersion only by applying expression \(\Delta \rho = \sqrt{(\Gamma^2 - \Gamma_{\exp}^2) / \alpha^2}\).

Here \(\Gamma > \Gamma_{\exp}\) stands for the actual absorber linewidth, while \(\Gamma_{\exp}\) is the corresponding linewidth in the absence of the modulation. The symbol \(\alpha\) is the previously defined calibration constant for the isomer shift, and \(\Delta \rho\) is the dispersion of the electron density on resonant nuclei [18].

### 3 SELECTED RESULTS

A commercial \(^{57}\)Co(Rh) sources were used for \(^{57}\)Fe spectroscopy. They were kept at room temperature. All reported shifts are reported against natural \(\alpha\)-Fe kept at room temperature for \(^{57}\)Fe spectroscopy.

3.1 Iron selenide

Essential results for the \(\text{Fe}_{1.01}\)Se compound with the superconducting transition at about 8 K are summarized below [19]. Spectra exhibit quadrupole split doublets with a small jump in the isomer shift at the tetragonal-orthorhombic transition. This jump corresponds to the lowering of the electron density on the iron nucleus in the \(C\text{mma}\) orthorhombic low temperature phase by \(0.02\text{el./a.u.}^3\) in comparison with the tetragonal \(P4/nmm\) phase at the same temperature. A transition occurs at about 105 K.
There are no traces of the magnetic order. Hence, the spectra were obtained in the longitudinal external magnetic field and they are shown in Figure 1. The applied fields exceeded the first critical field at temperatures of measurements. Due to the fact, that only very small volume of the sample retains superconductivity between first and second critical field almost all iron atoms are exposed to the applied field.

Hence, it was proven that the compound is truly diamagnetic and very hard to polarize by the external magnetic field, as the observed field is practically the same as applied field. This finding excludes exotic magnetically based coupling boson fields leading to the formation of the Bose quasi-particles and subsequently to the Bose condensate responsible for superconductivity.

3.2 CDW and EFGW sensitivity to the superconducting transition

Optimally doped ‘122’ compound Ba$_{0.6}$K$_{0.4}$Fe$_2$As$_2$ does not exhibit any magnetic order. The superconducting gap for this compound begins to open at 38 K and the gap is fully formed by 24 K provided there is neither external magnetic field nor hydrostatic pressure. It is worth noting that the superconductor is obtained by the hole doping of the parent compound BaFe$_2$As$_2$ [18]. On the other hand, the ‘1111’ superconductor SmFeAsO$_{0.91}$F$_{0.09}$ is obtained from the parent SmFeAsO by electron doping. The gap for the latter superconductor starts to open at 47 K and the gap formation is completed by 38 K. Unfortunately some traces of SDW appear for the latter case, but fortunately at about 20 K and below [20]. Figure 2 shows $^{57}$Fe spectra of the Ba$_{0.6}$K$_{0.4}$Fe$_2$As$_2$ compound collected around transition to the superconducting state (left panel), while the corresponding spectra of the SmFeAsO$_{0.91}$F$_{0.09}$ compound are shown in the right panel of Figure 2.

One can clearly see change of the spectrum shape at the gap opening and partial recovery upon full development of the gap. Changes have opposite character for the hole and electron doped sample.
Figure 3 shows evolution of the EFGW across superconducting transition and complete formation of the Bose condensate with corresponding variations in the electron density $\Delta \rho$ on the iron nuclei versus temperature.

Figure 2: $^{57}$Fe spectra for the optimally doped Ba$_{0.6}$K$_{0.4}$Fe$_2$As$_2$ compound around transition to the superconducting state (left panel) [18]. Right panel shows similar spectra of the SmFeAsO$_{1-x}$F$_x$ superconductor around transition to the superconducting state [20].

It is evident that changes have opposite signs depending on the addition to or removal of electrons from the system.
Figure 3: Shape of the EFGW for selected temperatures versus phase $\mathbf{q} \cdot \mathbf{r}$. Insets show corresponding normalized weights $w(\varepsilon - \varepsilon_0)$ of the quadrupole coupling constant $\varepsilon - \varepsilon_0$. Left panel shows EFGW for $\text{Ba}_{0.6}\text{K}_{0.4}\text{Fe}_2\text{As}_2$, while the right panel EFGW for $\text{SmFeAsO}_{0.9}\text{F}_{0.09}$. For the latter case one has $\varepsilon_0 = 0$. Lower part shows variation of the electron density $\Delta \rho$ on the iron nuclei during formation of the Bose condensate. Left panel shows results for $\text{Ba}_{0.6}\text{K}_{0.4}\text{Fe}_2\text{As}_2$ [18], while the right panel for $\text{SmFeAsO}_{0.9}\text{F}_{0.09}$ [20]. Dashed vertical lines mark superconducting transition temperature.
4 CONCLUSIONS

It is clear that superconducting and 3d magnetically ordered electronic systems are mutually exclusive, and no 3d intrinsic magnetic moments exist within superconductor. On the other hand, one has to allow for tunneling of the Bose condensate across magnetic regions and vice versa, as the 3d magnetism is of the itinerant character. Hence, it seems unlikely that magnetic excitations of any kind generate bosonic field responsible for coupling electrons into pairs.

Superconductors obtained by hole or electron doping from otherwise magnetic metallic material exhibiting itinerant 3d magnetism with significant magnetoelastic forces develop CDW and EFGW instead of structural transition. The latter charge waves are sensitive to the superconducting gap opening and complete formation. Changes are opposite for hole and electron doping.

REFERENCES


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